# Package: gpindex (via r-universe)

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Title Generalized Price and Quantity Indexes

Version 0.6.2

**Description** Tools to build and work with bilateral generalized-mean price indexes (and by extension quantity indexes), and indexes composed of generalized-mean indexes (e.g., superlative quadratic-mean indexes, GEKS). Covers the core mathematical machinery for making bilateral price indexes, computing price relatives, detecting outliers, and decomposing indexes, with wrappers for all common (and many uncommon) index-number formulas. Implements and extends many of the methods in Balk (2008, <doi:10.1017/CBO9780511720758>), von der Lippe (2007, <doi:10.3726/978-3-653-01120-3>), and the CPI manual (2020, <doi:10.5089/9781484354841.069>).

```
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Imports stats

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```

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2 back\_period

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back\_period

Offset a vector prices or quantities

# Description

For each product, compute either the position of the previous period (back period), or the position of the first period (base period). Useful when price information is stored in a table.

# Usage

```
back_period(period, product = gl(1, length(period)), match_first = TRUE)
base_period(period, product = gl(1, length(period)), match_first = TRUE)
```

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### **Arguments**

period A factor, or something that can be coerced into one, that gives the time period

for each transaction. The ordering of time periods follows the levels of period

to agree with cut().

product A factor, or something that can be coerced into one, that gives the product iden-

tifier for each transaction. The default is to assume that all transactions are for

the same product.

match\_first Should products in the first period match with themselves (the default)?

#### Value

Both functions return a numeric vector of indices for the back/base periods. With back\_period(), for all periods after the first, the resulting vector gives the location of the corresponding product in the previous period. With base\_period(), the resulting vector gives the location of the corresponding product in the first period. The locations are unchanged for the first time period if match\_first = TRUE, NA otherwise.

#### Note

By definition, there must be at most one transaction for each product in each time period to determine a back/base period. If multiple transactions correspond to a period-product pair, then the back/base period at a point in time is always the first position for that product in the previous period.

#### See Also

outliers for common methods to detect outliers for price relatives.

rs\_pairs in the **rsmatrix** package for making sales pairs.

```
df <- data.frame(
    price = 1:6,
    product = factor(c("a", "b")),
    period = factor(c(1, 1, 2, 2, 3, 3))
)
with(df, back_period(period, product))
# Make period-over-period price relatives
with(df, price / price[back_period(period, product)])
# Make fixed-base price relatives
with(df, price / price[base_period(period, product)])
# Change the base period with relevel()
with(df, price / price[base_period(relevel(period, "2"), product)])</pre>
```

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```
# Warning is given if the same product has multiple prices
# at any point in time
with(df, back_period(period))
```

balanced

Balanced operator

# **Description**

Makes a function balance the removal of NAs across multiple input vectors.

### Usage

```
balanced(f, ...)
```

# Arguments

f A function.

... Deprecated. Additional arguments to f that should *not* be balanced.

# Value

A function like f with a new argument na.rm. If na.rm = TRUE then complete.cases() is used to remove missing values across all inputs prior to calling f.

#### See Also

```
Other operators: grouped(), quantity_index()
```

```
p1 <- price6[[3]]
p0 <- price6[[2]]
q1 <- quantity6[[3]]
q0 <- quantity6[[2]]

# Balance missing values for a Fisher index

fisher <- balanced(fisher_index)
fisher(p1, p0, q1, replace(q0, 3, NA), na.rm = TRUE)
fisher_index(p1[-3], p0[-3], q1[-3], q0[-3])

# Operators can be combined, but some care may be needed

x <- 1:6
w <- c(1:5, NA)</pre>
```

```
f <- factor(rep(letters[1:2], each = 3))
grouped(\((x, w) balanced(fisher_mean)(x, w, na.rm = TRUE))(x, w, group = f)
balanced(grouped(fisher_mean))(x, w, group = f, na.rm = TRUE)</pre>
```

contributions

Percent-change contributions

# Description

Calculate additive percent-change contributions for generalized-mean price indexes, and indexes that nest two levels of generalized means consisting of an outer generalized mean and two inner generalized means (e.g., the Fisher index).

# Usage

```
contributions(r)
arithmetic_contributions(x, w = NULL)
geometric_contributions(x, w = NULL)
harmonic_contributions(x, w = NULL)
nested_contributions(r1, r2, t = c(1, 1))
nested_contributions2(r1, r2, t = c(1, 1))
fisher_contributions(x, w1 = NULL, w2 = NULL)
fisher_contributions2(x, w1 = NULL, w2 = NULL)
```

# **Arguments**

r	A finite number giving the order of the generalized mean.
x	A strictly positive numeric vector.
w, w1, w2	A strictly positive numeric vector of weights, the same length as $x$ . The default is to equally weight each element of $x$ .
r1	A finite number giving the order of the outer generalized mean.
r2	A pair of finite numbers giving the order of the inner generalized means.
t	A pair of strictly positive weights for the inner generalized means. The default is equal weights.

#### **Details**

The function contributions() is a simple wrapper for transmute\_weights(r, 1)() to calculate (additive) percent-change contributions for a price index based on a generalized mean of order r. It returns a function to compute a vector v(x, w) such that

```
generalized_mean(r)(x, w) - 1 == sum(v(x, w))
```

This generalizes the approach for calculating percent-change contributions in section 4.2 of Balk (2008) using the method by Martin (2021). The arithmetic\_contributions(), geometric\_contributions() and harmonic\_contributions() functions cover the most important cases (i.e., r = 1, r = 0, and r = -1).

The nested\_contributions() and nested\_contributions2() functions are the analog of contributions() for an index based on a nested generalized mean with two levels, like a Fisher index. They return a function that calculates the contribution of each element of x when a generalized mean of order r1 aggregates two generalized-mean indexes of x with orders r2, and weights w1 and w2.

Unlike the case of a generalized-mean index, there are several ways to make contributions for an index based on nested generalized means. nested\_contributions() uses a generalization of the algorithm in section 6 of Reinsdorf et al. (2002) by Martin (2021). nested\_contributions2() generalizes the van IJzeren decomposition for the Fisher index (Balk, 2008, section 4.2.2) by constructing a weighted average of the contributions for both of the inner means with the approach by Martin (2021). In most cases the results are broadly similar.

The fisher\_contributions() and fisher\_contributions2() functions correspond to nested\_contributions(0, c(1, -1))() and nested\_contributions2(0, c(1, -1))(), and are appropriate for calculating percent-change contributions for a Fisher index.

### Value

contributions() returns a function:

```
function(x, w = NULL){...}
```

This computes the additive contribution for each element of x in an index based on the generalized mean of order r with weights w.

nested\_contributions() and nested\_contributions2() return a function:

```
function(x, w1 = NULL, w2 = NULL){...}
```

This computes the additive contribution for each element of x when a generalized mean of order r1 aggregates a generalized-mean index of order r2[1] with weights w1 and a generalized-mean index of order r2[2] with weights w2.

arithmetic\_contributions(), geometric\_contributions(), and harmonic\_contributions() each return a numeric vector, the same length as x, giving the contribution of each element of x in an arithmetic, geometric, or harmonic index.

fisher\_contributions() and fisher\_contributions2() each return a numeric vector, the same length as x, giving the contribution of each element of x when a geometric mean aggregates an arithmetic mean of x with weights w1 and a harmonic mean of x with weights w2.

#### References

Balk, B. M. (2008). Price and Quantity Index Numbers. Cambridge University Press.

Hallerbach, W. G. (2005). An alternative decomposition of the Fisher index. *Economics Letters*, 86(2):147–152

Martin, S. (2021). A note on general decompositions for price indexes. *Prices Analytical Series*, Statistics Canada catalogue no. 62F0014M. Statistics Canada, Ottawa.

Reinsdorf, M. B., Diewert, W. E., and Ehemann, C. (2002). Additive decompositions for Fisher, Törnqvist and geometric mean indexes. *Journal of Economic and Social Measurement*, 28(1-2):51–61.

Webster, M. and Tarnow-Mordi, R. C. (2019). Decomposing multilateral price indexes into the contributions of individual commodities. *Journal of Official Statistics*, 35(2):461–486.

#### See Also

transmute\_weights() for the underlying implementation.

```
x <- 2:3
#---- Contributions for a geometric index ----
geometric_mean(x) - 1 # percent change in the Jevons index
geometric_contributions(x)
all.equal(geometric_mean(x) - 1, sum(geometric_contributions(x)))
# This works by first transmuting the weights in the geometric mean
# into weights for an arithmetic mean, then finding the contributions
# to the percent change
transmute_weights(0, 1)(x) * (x - 1)
# Not the only way to calculate contributions
transmute2 <- function(x) {</pre>
  m <- geometric_mean(x)</pre>
  (m - 1) / log(m) * log(x) / (x - 1) / length(x)
}
transmute2(x) * (x - 1) # not proportional to the method above
all.equal(sum(transmute2(x) * (x - 1)), geometric_mean(x) - 1)
# But these "transmuted" weights don't recover the geometric mean!
# Not a particularly good way to calculate contributions
isTRUE(all.equal(
  arithmetic_mean(x, transmute2(x)),
  geometric_mean(x)
```

```
))
# There are infinitely many ways to calculate contributions, but the
# weights from transmute_weights(0, 1)() are the *unique* weights that
# recover the geometric mean
perturb <- function(w, e) {</pre>
  w + c(e, -e) / (x - 1)
}
perturb(transmute2(x), 0.1) * (x - 1)
all.equal(
  sum(perturb(transmute2(x), 0.1) * (x - 1)),
  geometric_mean(x) - 1
)
isTRUE(all.equal(
  arithmetic_mean(x, perturb(transmute2(x), 0.1)),
  geometric_mean(x)
))
#---- Contributions for a Fisher index ----
p1 <- price6[[2]]
p0 <- price6[[1]]</pre>
q1 <- quantity6[[2]]
q0 <- quantity6[[1]]</pre>
# Percent-change contributions for the Fisher index in section 6 of
# Reinsdorf et al. (2002)
(con <- fisher_contributions(</pre>
  p1 / p0,
  index_weights("Laspeyres")(p0, q0),
  index_weights("Paasche")(p1, q1)
))
all.equal(sum(con), fisher_index(p1, p0, q1, q0) - 1)
# Not the only way
(con2 <- fisher_contributions2(</pre>
  p1 / p0,
  index_weights("Laspeyres")(p0, q0),
  index_weights("Paasche")(p1, q1)
))
all.equal(sum(con2), fisher_index(p1, p0, q1, q0) - 1)
# The same as the van IJzeren decomposition in section 4.2.2 of
# Balk (2008)
Qf <- quantity_index(fisher_index)(q1, q0, p1, p0)
Ql <- quantity_index(laspeyres_index)(q1, q0, p0)
```

```
wl <- scale_weights(index_weights("Laspeyres")(p0, q0))</pre>
wp <- scale_weights(index_weights("HybridPaasche")(p0, q1))</pre>
(Qf / (Qf + Q1) * w1 + Q1 / (Qf + Q1) * wp) * (p1 / p0 - 1)
# Similar to the method in section 2 of Reinsdorf et al. (2002),
# although those contributions aren't based on weights that sum to 1
Pf <- fisher_index(p1, p0, q1, q0)
Pl <- laspeyres_index(p1, p0, q0)
(1 / (1 + Pf) * wl + Pl / (1 + Pf) * wp) * (p1 / p0 - 1)
# Also similar to the decomposition by Hallerbach (2005), noting that
# the Euler weights are close to unity
Pp <- paasche_index(p1, p0, q1)</pre>
(0.5 * sqrt(Pp / Pl) * wl + 0.5 * sqrt(Pl / Pp) * wp) * (p1 / p0 - 1)
#---- Contributions for other types of indexes ----
# A function to get contributions for any superlative quadratic mean of
# order 'r' index
superlative_contributions <- function(r) {</pre>
  nested\_contributions(0, c(r / 2, -r / 2))
}
# Can be used to decompose the implict Walsh index
superlative_contributions(1)(
  p1 / p0,
  index_weights("Laspeyres")(p0, q0),
  index_weights("Paasche")(p1, q1)
)
# Works for other types of indexes, like the harmonic
# Laspeyres Paasche index
hlp_contributions <- nested_contributions(-1, c(1, -1))</pre>
hlp_contributions(
  p1 / p0,
  index_weights("Laspeyres")(p0, q0),
  index_weights("Paasche")(p1, q1)
)
# Or the AG mean index (tau = 0.25)
agmean_contributions <- nested_contributions(1, c(0, 1), c(0.25, 0.75))
agmean_contributions(
  p1 / p0,
  index_weights("Laspeyres")(p0, q0),
```

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```
index_weights("Laspeyres")(p0, q0)
)

# Or the Balk-Walsh index

bw_contributions <- nested_contributions(0, c(0.5, -0.5))
bw_contributions(p1 / p0)</pre>
```

extended\_mean

Extended mean

# **Description**

Calculate a generalized logarithmic mean / extended mean.

# Usage

```
extended_mean(r, s)
generalized_logmean(r)
logmean(a, b, tol = .Machine$double.eps^0.5)
```

### **Arguments**

r, s	A finite number giving the order of the generalized logarithmic mean / extended
	mean.
a, b	A strictly positive numeric vector.
tol	The tolerance used to determine if a == b.

#### **Details**

The function extended\_mean() returns a function to compute the component-wise extended mean of a and b of orders r and s. See Bullen (2003, p. 393) for a definition. This is also called the difference mean, Stolarsky mean, or extended mean-value mean.

The function generalized\_logmean() returns a function to compute the component-wise generalized logarithmic mean of a and b of order r. See Bullen (2003, p. 385) for a definition, or https://en.wikipedia.org/wiki/Stolarsky\_mean. The generalized logarithmic mean is a special case of the extended mean, corresponding to extended\_mean(r, 1)(), but is more commonly used for price indexes.

The function logmean() returns the ordinary component-wise logarithmic mean of a and b, and corresponds to generalized\_logmean(1)().

Both a and b should be strictly positive. This is not enforced, but the results may not make sense when the generalized logarithmic mean / extended mean is not defined. The usual recycling rules apply when a and b are not the same length.

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By definition, the generalized logarithmic mean / extended mean of a and b is a when a == b. The tol argument is used to test equality by checking if  $abs(a - b) \le tol$ . The default value is the same as all.equal(). Setting tol = 0 tests for exact equality, but can give misleading results when a and b are computed values. In some cases it's useful to multiply tol by a scale factor, such as max(abs(a), abs(b)). This often doesn't matter when making price indexes, however, as a and b are usually around 1.

#### Value

generalized\_logmean() and extended\_mean() return a function:

```
function(a, b, tol = .Machine$double.eps^0.5){...}
```

This computes the component-wise generalized logarithmic mean of order r, or the extended mean of orders r and s, of a and b.

logmean() returns a numeric vector, the same length as max(length(a), length(b)), giving the component-wise logarithmic mean of a and b.

#### Note

generalized\_logmean() can be defined on the extended real line, so that r = -Inf / Inf returns pmin()/pmax(), to agree with the definition in, e.g., Bullen (2003). This is not implemented, and r must be finite as in the original formulation by Stolarsky (1975).

# References

Balk, B. M. (2008). Price and Quantity Index Numbers. Cambridge University Press.

Bullen, P. S. (2003). *Handbook of Means and Their Inequalities*. Springer Science+Business Media.

Stolarsky, K. B. (1975). Generalizations of the Logarithmic Mean. *Mathematics Magazine*, 48(2): 87-92.

#### See Also

 $transmute\_weights()$  uses the extended mean to turn a generalized mean of order r into a generalized mean of order s.

Other means: generalized\_mean(), lehmer\_mean(), nested\_mean()

```
x <- 8:5
y <- 1:4
#---- Comparing logarithmic means and generalized means ----
# The arithmetic and geometric means are special cases of the
# generalized logarithmic mean
all.equal(generalized_logmean(2)(x, y), (x + y) / 2)</pre>
```

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```
all.equal(generalized_logmean(-1)(x, y), sqrt(x * y))
# The logarithmic mean lies between the arithmetic and geometric means
# because the generalized logarithmic mean is increasing in r
all(logmean(x, y) < (x + y) / 2) &
  all(logmean(x, y) > sqrt(x * y))
# The harmonic mean cannot be expressed as a logarithmic mean, but can
# be expressed as an extended mean
all.equal(extended_mean(-2, -1)(x, y), 2 / (1 / x + 1 / y))
# The quadratic mean is also a type of extended mean
all.equal(extended_mean(2, 4)(x, y), sqrt(x^2 / 2 + y^2 / 2))
# As are heronian and centroidal means
all.equal(
  extended_mean(0.5, 1.5)(x, y),
  (x + sqrt(x * y) + y) / 3
)
all.equal(
  extended_mean(2, 3)(x, y),
  2 / 3 * (x^2 + x * y + y^2) / (x + y)
#---- Approximating the logarithmic mean ----
# The logarithmic mean can be approximated as a convex combination of
# the arithmetic and geometric means that gives more weight to the
# geometric mean
approx1 <- 1 / 3 * (x + y) / 2 + 2 / 3 * sqrt(x * y)
approx2 <- ((x + y) / 2)^{(1 / 3)} * (sqrt(x * y))^{(2 / 3)}
approx1 - logmean(x, y) # always a positive approximation error
approx2 - logmean(x, y) # a negative approximation error
# A better approximation
correction <- (log(x / y) / pi)^4 / 32
approx1 / (1 + correction) - logmean(x, y)
#---- Some identities ----
# A useful identity for turning an additive change into a proportionate
# change
all.equal(logmean(x, y) * log(x / y), x - y)
# Works for other orders, too
```

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```
r <- 2
all.equal(
  generalized_logmean(r)(x, y)^(r - 1) * (r * (x - y)),
  (x^r - y^r)
)
# Some other identities
all.equal(
  generalized_logmean(-2)(1, 2),
  (harmonic_mean(1:2) * geometric_mean(1:2)^2)^(1 / 3)
all.equal(
  generalized_logmean(0.5)(1, 2),
  (arithmetic_mean(1:2) + geometric_mean(1:2)) / 2
)
all.equal(
  logmean(1, 2),
  geometric_mean(1:2)^2 * logmean(1, 1 / 2)
#---- Integral representations of the logarithmic mean ----
logmean(2, 3)
integrate(function(t) 2^{(1 - t)} * 3^t, 0, 1)$value
1 / integrate(function(t) 1 / (2 * (1 - t) + 3 * t), 0, 1)$value
```

factor\_weights

Factor weights

# **Description**

Factor weights to turn the generalized mean of a product into the product of generalized means. Useful for price-updating the weights in a generalized-mean index.

# Usage

```
factor_weights(r)
update_weights(x, w = NULL)
```

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# Arguments

	A C	1		.1 1	C .1	1' 1
r	A finite n	umber	giving	the orde	er of the	generalized mean.

x A strictly positive numeric vector.

w A strictly positive numeric vector of weights, the same length as x. The default is to equally weight each element of x.

### **Details**

The function factor\_weights(r) returns a function to compute weights u(x, w) such that

```
generalized_mean(r)(x * y, w) == generalized_mean(r)(x, w) * generalized_mean(r)(y, u(x, w))
```

This generalizes the result in section C.5 of Chapter 9 of the PPI Manual for chaining the Young index, and gives a way to chain generalized-mean price indexes over time.

Factoring weights with r = 1 sometimes gets called price-updating weights; update\_weights() simply calls factor\_weights(1)().

Factoring weights return a value that is the same length as x, so any missing values in x or the weights will return NA. Unless all values are NA, however, the result for will still satisfy the above identity when na.rm = TRUE.

# Value

```
factor_weights() return a function:
function(x, w = NULL){...}
update_weights() returns a numeric vector the same length as x.
```

# References

ILO, IMF, OECD, UNECE, and World Bank. (2004). *Producer Price Index Manual: Theory and Practice*. International Monetary Fund.

# See Also

```
generalized_mean() for the generalized mean.
grouped() to make these functions operate on grouped data.
Other weights functions: scale_weights(), transmute_weights()
```

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### **Examples**

```
x <- 1:3
y <- 4:6
w <- 3:1
# Factor the harmonic mean by chaining the calculation
harmonic_mean(x * y, w)
harmonic_mean(x, w) * harmonic_mean(y, factor_weights(-1)(x, w))
# The common case of an arithmetic mean
arithmetic_mean(x * y, w)
arithmetic_mean(x, w) * arithmetic_mean(y, update_weights(x, w))
# In cases where x and y have the same order, Chebyshev's
# inequality implies that the chained calculation is too small
arithmetic_mean(x * y, w) >
arithmetic_mean(x, w) * arithmetic_mean(y, w)
```

geks

GEKS index

# **Description**

Calculate a generalized inter-temporal GEKS price index over a rolling window.

### Usage

```
geks(f, r = 0)
tornqvist_geks(
 р,
  q,
 period,
 product,
 window = nlevels(period),
  n = window - 1L,
  na.rm = FALSE
)
fisher_geks(
  р,
  q,
  period,
  product,
 window = nlevels(period),
```

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```
n = window - 1L,
na.rm = FALSE
)

walsh_geks(
p,
q,
period,
product,
window = nlevels(period),
n = window - 1L,
na.rm = FALSE
)
```

# Arguments

f	A price index function that uses information on both base and current-period prices and quantities, and satisfies the time-reversal test. Usually a Törnqvist, Fisher, or Walsh index.
r	A finite number giving the order of the generalized mean used to average price indexes over the rolling window. The default uses a geometric mean.
р	A numeric vector of prices, the same length as q.
q	A numeric vector of quantities, the same length as p.
period	A factor, or something that can be coerced into one, that gives the corresponding time period for each element in p and q. The ordering of time periods follows the levels of period to agree with cut().
product	A factor, or something that can be coerced into one, that gives the corresponding product identifier for each element in p and q.
window	A positive integer giving the length of the rolling window. The default is a window that encompasses all periods in period. Non-integers are truncated towards zero.
n	A positive integer giving the length of the index series for each window, starting from the end of the window. For example, if there are 13 periods in window, setting n = 1 gives the index for period 13. The default gives an index for each period in window. Non-integers are truncated towards zero.
na.rm	Passed to f to control if missing values are removed.

# Value

```
geks() returns a function:
```

This calculates a period-over-period GEKS index with the desired index-number formula, returning a list for each window with a named-numeric vector of index values.

tornqvist\_geks(), fisher\_geks(), and walsh\_geks() each return a list with a named numeric vector giving the value of the respective period-over-period GEKS index for each window.

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#### Note

Like back\_period(), if multiple prices correspond to a period-product pair, then the back price at a point in time is always the first price for that product in the previous period. Unlike a bilateral index, however, duplicated period-product pairs can have more subtle implications for a multilateral index.

### References

Balk, B. M. (2008). Price and Quantity Index Numbers. Cambridge University Press.

IMF, ILO, Eurostat, UNECE, OECD, and World Bank. (2020). *Consumer Price Index Manual: Concepts and Methods*. International Monetary Fund.

Ivancic, L., Diewert, W. E., and Fox, K. J. (2011). Scanner data, time aggregation and the construction of price indexes. *Journal of Econometrics*, 161(1): 24–35.

#### See Also

GEKSIndex() in the **indexNumR** package for an implementation of the GEKS index with more options.

Other price index functions: index\_weights(), price\_indexes, splice\_index()

```
price <- 1:10
quantity <- 10:1
period < - rep(1:5, 2)
product <- rep(letters[1:2], each = 5)</pre>
cumprod(tornqvist_geks(price, quantity, period, product)[[1]])
# Calculate the index over a rolling window
(tg <- tornqvist_geks(price, quantity, period, product, window = 3))</pre>
# Use a movement splice to combine the indexes in each window
splice_index(tg, 2)
# ... or use a mean splice
splice_index(tg)
#---- Missing data ----
quantity[2] <- NA
# Use all non-missing data
fisher_geks(price, quantity, period, product, na.rm = TRUE)
# Remove records with any missing data
```

```
fg <- geks(balanced(fisher_index))
fg(price, quantity, period, product, na.rm = TRUE)
#---- Make a Jevons GEKS index ----
jevons_geks <- geks(\(p1, p0, ..., na.rm\) jevons_index(p1, p0, na.rm\))
jevons_geks(price, quantity, period, product)</pre>
```

generalized\_mean

Generalized mean

### **Description**

Calculate a weighted generalized mean.

# Usage

```
generalized_mean(r)
arithmetic_mean(x, w = NULL, na.rm = FALSE)
geometric_mean(x, w = NULL, na.rm = FALSE)
harmonic_mean(x, w = NULL, na.rm = FALSE)
```

#### **Arguments**

r A finite number giving the order of the generalized mean.

x A strictly positive numeric vector.

A strictly positive numeric vector of weights, the same length as x. The default

is to equally weight each element of x.

na.rm Should missing values in x and w be removed? By default missing values in x or

w return a missing value.

#### **Details**

The function generalized\_mean() returns a function to compute the generalized mean of x with weights w and exponent r (i.e.,  $\prod_{i=1}^n x_i^{w_i}$  when r=0 and  $(\sum_{i=1}^n w_i x_i^r)^{1/r}$  otherwise). This is also called the power mean, Hölder mean, or  $l_p$  mean. See Bullen (2003, p. 175) for a definition, or https://en.wikipedia.org/wiki/Generalized\_mean. The generalized mean is the solution to the optimal prediction problem: choose m to minimize  $\sum_{i=1}^n w_i \left[\log(x_i) - \log(m)\right]^2$  when r=0,  $\sum_{i=1}^n w_i \left[x_i^r - m^r\right]^2$  otherwise.

The functions arithmetic\_mean(), geometric\_mean(), and harmonic\_mean() compute the arithmetic, geometric, and harmonic (or subcontrary) means, also known as the Pythagorean means.

These are the most useful means for making price indexes, and correspond to setting r = 1, r = 0, and r = -1 in generalized\_mean().

Both x and w should be strictly positive (and finite), especially for the purpose of making a price index. This is not enforced, but the results may not make sense if the generalized mean is not defined. There are two exceptions to this.

- 1. The convention in Hardy et al. (1952, p. 13) is used in cases where x has zeros: the generalized mean is 0 whenever w is strictly positive and r < 0. (The analogous convention holds whenever at least one element of x is Inf: the generalized mean is Inf whenever w is strictly positive and r > 0.)
- 2. Some authors let w be non-negative and sum to 1 (e.g., Sydsaeter et al., 2005, p. 47). If w has zeros, then the corresponding element of x has no impact on the mean whenever x is strictly positive. Unlike weighted.mean(), however, zeros in w are not strong zeros, so infinite values in x will propagate even if the corresponding elements of w are zero.

The weights are scaled to sum to 1 to satisfy the definition of a generalized mean. There are certain price indexes where the weights should not be scaled (e.g., the Vartia-I index); use sum() for these cases.

The underlying calculation returned by generalized\_mean() is mostly identical to weighted.mean(), with one important exception: missing values in the weights are not treated differently than missing values in x. Setting na.rm = TRUE drops missing values in both x and w, not just x. This ensures that certain useful identities are satisfied with missing values in x. In most cases arithmetic\_mean() is a drop-in replacement for weighted.mean().

### Value

generalized\_mean() returns a function:

```
function(x, w = NULL, na.rm = FALSE){...}
```

This computes the generalized mean of order r of x with weights w.

arithmetic\_mean(), geometric\_mean(), and harmonic\_mean() each return a numeric value for the generalized means of order 1, 0, and -1.

#### Note

generalized\_mean() can be defined on the extended real line, so that r = -Inf / Inf returns min()/max(), to agree with the definition in, e.g., Bullen (2003). This is not implemented, and r must be finite.

There are a number of existing functions for calculating *unweighted* geometric and harmonic means, namely the geometric.mean() and harmonic.mean() functions in the **psych** package, the geomean() function in the **FSA** package, the GMean() and HMean() functions in the **DescTools** package, and the geoMean() function in the **EnvStats** package. Similarly, the ci\_generalized\_mean() function in the **Compind** package calculates an *unweighted* generalized mean.

#### References

Bullen, P. S. (2003). *Handbook of Means and Their Inequalities*. Springer Science+Business Media.

Fisher, I. (1922). The Making of Index Numbers. Houghton Mifflin Company.

Hardy, G., Littlewood, J. E., and Polya, G. (1952). *Inequalities* (2nd edition). Cambridge University Press.

IMF, ILO, Eurostat, UNECE, OECD, and World Bank. (2020). *Consumer Price Index Manual: Concepts and Methods*. International Monetary Fund.

Lord, N. (2002). Does Smaller Spread Always Mean Larger Product? *The Mathematical Gazette*, 86(506): 273-274.

Sydsaeter, K., Strom, A., and Berck, P. (2005). *Economists' Mathematical Manual* (4th edition). Springer.

### See Also

 $transmute\_weights()$  transforms the weights to turn a generalized mean of order r into a generalized mean of order s.

factor\_weights() calculates the weights to factor a mean of products into a product of means.

price\_indexes and quantity\_index() for simple wrappers that use generalized\_mean() to calculate common indexes.

back\_period()/base\_period() for a simple utility function to turn prices in a table into price relatives.

Other means: extended\_mean(), lehmer\_mean(), nested\_mean()

```
x <- 1:3
w <- c(0.25, 0.25, 0.5)
#---- Common generalized means ----
# Arithmetic mean
arithmetic_mean(x, w) # same as weighted.mean(x, w)
# Geometric mean
geometric_mean(x, w) # same as prod(x^w)
# Harmonic mean
harmonic_mean(x, w) # same as 1 / weighted.mean(1 / x, w)
# Quadratic mean / root mean square
generalized_mean(2)(x, w)</pre>
```

```
# Cubic mean
# Notice that this is larger than the other means so far because
# the generalized mean is increasing in r
generalized_mean(3)(x, w)
#---- Comparing the Pythagorean means ----
# The dispersion between the arithmetic, geometric, and harmonic
# mean usually increases as the variance of 'x' increases
x \leftarrow c(1, 3, 5)
y < -c(2, 3, 4)
var(x) > var(y)
arithmetic_mean(x) - geometric_mean(x)
arithmetic_mean(y) - geometric_mean(y)
geometric_mean(x) - harmonic_mean(x)
geometric_mean(y) - harmonic_mean(y)
# But the dispersion between these means is only bounded by the
# variance (Bullen, 2003, p. 156)
arithmetic_mean(x) - geometric_mean(x) >= 2 / 3 * var(x) / (2 * max(x))
arithmetic_mean(x) - geometric_mean(x) \le 2 / 3 * var(x) / (2 * min(x))
# Example by Lord (2002) where the dispersion decreases as the variance
# increases, counter to the claims by Fisher (1922, p. 108) and the
# CPI manual (par. 1.14)
x \leftarrow (5 + c(sqrt(5), -sqrt(5), -3)) / 4
y \leftarrow (16 + c(7 * sqrt(2), -7 * sqrt(2), 0)) / 16
var(x) > var(y)
arithmetic_mean(x) - geometric_mean(x)
arithmetic_mean(y) - geometric_mean(y)
geometric_mean(x) - harmonic_mean(x)
geometric_mean(y) - harmonic_mean(y)
# The "bias" in the arithmetic and harmonic indexes is also smaller in
# this case, counter to the claim by Fisher (1922, p. 108)
arithmetic_mean(x) * arithmetic_mean(1 / x) - 1
arithmetic_mean(y) * arithmetic_mean(1 / y) - 1
harmonic_mean(x) * harmonic_mean(1 / x) - 1
harmonic_mean(y) * harmonic_mean(1 / y) - 1
#---- Missing values ----
```

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```
w[2] <- NA
arithmetic_mean(x, w, na.rm = TRUE) # drop the second observation
weighted.mean(x, w, na.rm = TRUE) # still returns NA</pre>
```

grouped

Grouped operator

# **Description**

Make a function applicable to grouped data.

# Usage

```
grouped(f, ...)
```

# **Arguments**

f A function.

... Deprecated. Additional arguments to f that should *not* be treated as grouped.

# Value

A function like f with a new argument group. This accepts a factor to split all other arguments in f into groups before applying f to each group and combining the results. It is similar to ave(), but more general.

### See Also

Other operators: balanced(), quantity\_index()

```
p1 <- price6[[3]]
p0 <- price6[[2]]
q1 <- quantity6[[3]]
q0 <- quantity6[[2]]

# Calculate Tornqvist weights for two groups

f <- factor(rep(letters[1:2], each = 3))
tornqvist_weights <- grouped(index_weights("Tornqvist"))
tornqvist_weights(p1, p0, q1, q0, group = f)

# Calculate a mean like ave(), but with weights
x <- 1:6</pre>
```

```
w <- c(1:5, NA)
grouped_mean <- grouped(\(x, w\)) geometric_mean(x, w, na.rm = TRUE))
grouped_mean(x, w, group = f)

# Redistribute weights

w1 <- c(2, 4)
w2 <- 1:6

harmonic_mean(mapply(harmonic_mean, split(x, f), split(w2, f)), w1)

wr <- grouped(scale_weights)(w2, group = f) * w1[f]
harmonic_mean(x, wr)</pre>
```

index\_weights

Index weights

### **Description**

Calculate weights for a variety of different price indexes.

# Usage

```
index_weights(
  type = c("Carli", "Jevons", "Coggeshall", "Dutot", "Laspeyres", "HybridLaspeyres",
   "LloydMoulton", "Palgrave", "Paasche", "HybridPaasche", "Drobisch", "Unnamed",
   "Tornqvist", "Walsh1", "Walsh2", "MarshallEdgeworth", "GearyKhamis", "Vartia1",
   "MontgomeryVartia", "Vartia2", "SatoVartia", "Theil", "Rao", "Lowe", "Young",
   "HybridCSWD")
)
```

# **Arguments**

type

The name of the index. See details for the possible types of indexes.

### **Details**

The index\_weights() function returns a function to calculate weights for a variety of price indexes. Weights for the following types of indexes can be calculated.

- · Carli / Jevons / Coggeshall
- Dutot
- Laspeyres / Lloyd-Moulton
- Hybrid Laspeyres (for use in a harmonic mean)
- · Paasche / Palgrave
- Hybrid Paasche (for use in an arithmetic mean)

- Törnqvist / Unnamed
- Drobisch
- Walsh-I (for an arithmetic Walsh index)
- Walsh-II (for a geometric Walsh index)
- · Marshall-Edgeworth
- · Geary-Khamis
- Montgomery-Vartia / Vartia-I
- Sato-Vartia / Vartia-II
- Theil
- Rao
- Lowe
- Young
- Hybrid-CSWD

The weights need not sum to 1, as this normalization isn't always appropriate (i.e., for the Vartia-I weights).

### Value

A function of current and base period prices/quantities that calculates the relevant weights.

### Note

Naming for the indexes and weights generally follows the CPI manual (2020), Balk (2008), von der Lippe (2007), and Selvanathan and Rao (1994). In several cases two or more names correspond to the same weights (e.g., Paasche and Palgrave, or Sato-Vartia and Vartia-II). The calculations are given in the examples.

# References

Balk, B. M. (2008). Price and Quantity Index Numbers. Cambridge University Press.

IMF, ILO, Eurostat, UNECE, OECD, and World Bank. (2020). *Consumer Price Index Manual: Concepts and Methods*. International Monetary Fund.

von der Lippe, P. (2007). Index Theory and Price Statistics. Peter Lang.

Selvanathan, E. A. and Rao, D. S. P. (1994). Index Numbers: A Stochastic Approach. MacMillan.

#### See Also

```
update_weights() for price-updating weights.
quantity_index() to remap the arguments in these functions for a quantity index.
Other price index functions: geks(), price_indexes, splice_index()
```

```
p0 <- price6[[2]]</pre>
p1 <- price6[[3]]
q0 <- quantity6[[2]]</pre>
q1 <- quantity6[[3]]</pre>
pb <- price6[[1]]</pre>
qb <- quantity6[[1]]</pre>
#---- Making the weights for different indexes ----
# Explicit calculation for each of the different weights
# Carli/Jevons/Coggeshall
all.equal(index_weights("Carli")(p1), rep(1, length(p0)))
# Dutot
all.equal(index_weights("Dutot")(p0), p0)
# Laspeyres / Lloyd-Moulton
all.equal(index_weights("Laspeyres")(p0, q0), p0 * q0)
# Hybrid Laspeyres
all.equal(index_weights("HybridLaspeyres")(p1, q0), p1 * q0)
# Paasche / Palgrave
all.equal(index_weights("Paasche")(p1, q1), p1 * q1)
# Hybrid Paasche
all.equal(index_weights("HybridPaasche")(p0, q1), p0 * q1)
# Tornqvist / Unnamed
all.equal(
  index_weights("Tornqvist")(p1, p0, q1, q0),
  0.5 * p0 * q0 / sum(p0 * q0) + 0.5 * p1 * q1 / sum(p1 * q1)
# Drobisch
all.equal(
  index_weights("Drobisch")(p1, p0, q1, q0),
  0.5 * p0 * q0 / sum(p0 * q0) + 0.5 * p0 * q1 / sum(p0 * q1)
)
# Walsh-I
all.equal(
```

```
index_weights("Walsh1")(p0, q1, q0),
  p0 * sqrt(q0 * q1)
# Marshall-Edgeworth
all.equal(
  index_weights("MarshallEdgeworth")(p0, q1, q0),
  p0 * (q0 + q1)
# Geary-Khamis
all.equal(
  index_weights("GearyKhamis")(p0, q1, q0),
  p0 / (1 / q0 + 1 / q1)
)
# Montgomery-Vartia / Vartia-I
all.equal(
  index_weights("MontgomeryVartia")(p1, p0, q1, q0),
  logmean(p0 * q0, p1 * q1) / logmean(sum(p0 * q0), sum(p1 * q1))
)
# Sato-Vartia / Vartia-II
all.equal(
  index_weights("SatoVartia")(p1, p0, q1, q0),
  logmean(p0 * q0 / sum(p0 * q0), p1 * q1 / sum(p1 * q1))
)
# Walsh-II
all.equal(
  index_weights("Walsh2")(p1, p0, q1, q0),
  sqrt(p0 * q0 * p1 * q1)
)
# Theil
all.equal(index_weights("Theil")(p1, p0, q1, q0), {
  w0 <- scale_weights(p0 * q0)</pre>
 w1 \leftarrow scale\_weights(p1 * q1)
  (w0 * w1 * (w0 + w1) / 2)^{(1 / 3)}
})
# Rao
all.equal(index_weights("Rao")(p1, p0, q1, q0), \{
  w0 <- scale_weights(p0 * q0)</pre>
  w1 <- scale_weights(p1 * q1)
  w0 * w1 / (w0 + w1)
```

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```
# Lowe
all.equal(index_weights("Lowe")(p0, qb), p0 * qb)
# Young
all.equal(index_weights("Young")(pb, qb), pb * qb)
# Hybrid CSWD (to approximate a CSWD index)
all.equal(index_weights("HybridCSWD")(p1, p0), sqrt(p0 / p1))
```

lehmer\_mean

Lehmer mean

#### **Description**

Calculate a weighted Lehmer mean.

# Usage

```
lehmer_mean(r)
contraharmonic_mean(x, w = NULL, na.rm = FALSE)
```

### **Arguments**

na.rm

r A finite number giving the order of the Lehmer mean.

x A strictly positive numeric vector.

w A strictly positive numeric vector of weights, the same length as x. The default is to equally weight each element of x.

Should missing values in x and w be removed? By default missing values in x or

w return a missing value.

#### **Details**

The function lehmer\_mean() returns a function to compute the Lehmer mean of order r of x with weights w, which is calculated as the arithmetic mean of x with weights  $wx^{r-1}$ . This is also called the counter-harmonic mean or generalized anti-harmonic mean. See Bullen (2003, p. 245) for a definition, or https://en.wikipedia.org/wiki/Lehmer\_mean.

The Lehmer mean of order 2 is sometimes called the contraharmonic (or anti-harmonic) mean. The function contraharmonic\_mean() simply calls lehmer\_mean(2)(). Like the generalized mean, the contraharmonic mean is the solution to an optimal prediction problem: choose m to minimize

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 $\sum_{i=1}^{n} w_i \left( \frac{x_i}{m} - 1 \right)^2$ . The Lehmer mean of order -1 has a similar interpretation, replacing  $\frac{x_i}{m}$  with  $\frac{m}{x_i}$ , and together these bound the harmonic and arithmetic means.

The Lehmer mean is an alternative to the generalized mean that generalizes the Pythagorean means. The function lehmer\_mean(1)() is identical to arithmetic\_mean(), lehmer\_mean(0)() is identical to harmonic\_mean(), and lehmer\_mean(0.5)() is identical to geometric\_mean() with two values and no weights. See von der Lippe (2015) for more details on the use of these means for making price indexes.

#### Value

```
lehmer_mean() returns a function:
```

```
function(x, w = NULL, na.rm = FALSE){...}
```

This computes the Lehmer mean of order r of x with weights w.

contraharmonic\_mean() returns a numeric value for the Lehmer mean of order 2.

#### Note

lehmer\_mean() can be defined on the extended real line, so that r = -Inf / Inf returns min()/max(), to agree with the definition in, e.g., Bullen (2003). This is not implemented, and r must be finite.

### References

Bullen, P. S. (2003). *Handbook of Means and Their Inequalities*. Springer Science+Business Media.

Lehmer, D. H. (1971). On the Compounding of Certain Means. *Journal of Mathematical Analysis and Applications*, 36(1): 183-200.

von der Lippe, P. (2015). Generalized Statistical Means and New Price Index Formulas, Notes on some unexplored index formulas, their interpretations and generalizations. Munich Personal RePEc Archive paper no. 64952.

# See Also

Other means: extended\_mean(), generalized\_mean(), nested\_mean()

```
x <- 2:3
w <- c(0.25, 0.75)

#---- The Pythagorean means are special cases of the Lehmer mean ----
all.equal(lehmer_mean(1)(x, w), arithmetic_mean(x, w))
all.equal(lehmer_mean(0)(x, w), harmonic_mean(x, w))
all.equal(lehmer_mean(0.5)(x), geometric_mean(x))
#---- Comparing Lehmer means and generalized means ----</pre>
```

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```
# When r < 1, the generalized mean is larger than the corresponding
lehmer_mean(-1)(x, w) < generalized_mean(-1)(x, w)
# The reverse is true when r > 1
lehmer_mean(3)(x, w) > generalized_mean(3)(x, w)
# This implies the contraharmonic mean is larger than the quadratic
# mean, and therefore the Pythagorean means
contraharmonic_mean(x, w) > arithmetic_mean(x, w)
contraharmonic_mean(x, w) > geometric_mean(x, w)
contraharmonic_mean(x, w) > harmonic_mean(x, w)
# ... and the logarithmic mean
contraharmonic_mean(2:3) > logmean(2, 3)
# The difference between the arithmetic mean and contraharmonic mean
\# is proportional to the variance of x
weighted_var <- function(x, w) {</pre>
 arithmetic_mean((x - arithmetic_mean(x, w))^2, w)
arithmetic_mean(x, w) + weighted_var(x, w) / arithmetic_mean(x, w)
contraharmonic_mean(x, w)
#---- Changing the order of the mean ----
# It is easy to modify the weights to turn a Lehmer mean of order r
# into a Lehmer mean of order s because the Lehmer mean can be
# expressed as an arithmetic mean
r <- 2
s <- -3
lehmer_mean(r)(x, w)
lehmer_mean(s)(x, w * x^{(r - 1)} / x^{(s - 1)})
# The weights can also be modified to turn a Lehmer mean of order r
# into a generalized mean of order s
lehmer_mean(r)(x, w)
generalized_mean(s)(x, transmute_weights(1, s)(x, w * x^{(r-1)}))
# ... and vice versa
lehmer_mean(r)(x, transmute_weights(s, 1)(x, w) / x^{(r-1)})
generalized_mean(s)(x, w)
#---- Percent-change contributions ----
```

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```
# Percent-change contributions for a price index based on the Lehmer # mean are easy to calculate scale\_weights(w * x^{(r-1)}) * (x-1)
```

nested\_mean

Nested generalized mean

# Description

Calculate the (outer) generalized mean of two (inner) generalized means (i.e., crossing generalized means).

# Usage

```
nested_mean(r1, r2, t = c(1, 1))
fisher_mean(x, w1 = NULL, w2 = NULL, na.rm = FALSE)
```

# **Arguments**

r1	A finite number giving the order of the outer generalized mean.
r2	A pair of finite numbers giving the order of the inner generalized means.
t	A pair of strictly positive weights for the inner generalized means. The default is equal weights.
X	A strictly positive numeric vector.
w1, w2	A strictly positive numeric vector of weights, the same length as x. The default is to equally weight each element of x.
na.rm	Should missing values in x, w1, and w2 be removed? By default missing values in x, w1, or w2 return a missing value.

# Value

nested\_mean() returns a function:

```
function(x, w1 = NULL, w2 = NULL, na.rm = FALSE){...}
```

This computes the generalized mean of order r1 of the generalized mean of order r2[1] of x with weights w1 and the generalized mean of order r2[2] of x with weights w2.

fisher\_mean() returns a numeric value for the geometric mean of the arithmetic and harmonic means (i.e., r1 = 0 and r2 = c(1, -1)).

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#### Note

There is some ambiguity about how to remove missing values in w1 or w2 when na.rm = TRUE. The approach here is to remove missing values when calculating each of the inner means individually, rather than removing all missing values prior to any calculations. This means that a different number of data points could be used to calculate the inner means. Use the balanced() operator to balance missing values across w1 and w2 prior to any calculations.

#### References

Diewert, W. E. (1976). Exact and superlative index numbers. *Journal of Econometrics*, 4(2): 114–145.

ILO, IMF, OECD, UNECE, and World Bank. (2004). *Producer Price Index Manual: Theory and Practice*. International Monetary Fund.

Lent, J. and Dorfman, A. H. (2009). Using a weighted average of base period price indexes to approximate a superlative index. *Journal of Official Statistics*, 25(1):139–149.

#### See Also

nested\_contributions() for percent-change contributions for indexes based on nested generalized means, like the Fisher index.

Other means: extended\_mean(), generalized\_mean(), lehmer\_mean()

```
x <- 1:3
w1 <- 4:6
w2 <- 7:9
#---- Making superlative indexes ----
# A function to make the superlative quadratic mean price index by
# Diewert (1976) as a product of generalized means
quadratic_mean_index <- function(r) nested_mean(0, c(r / 2, -r / 2))</pre>
quadratic_mean_index(2)(x, w1, w2)
# The arithmetic AG mean index by Lent and Dorfman (2009)
agmean_index <- function(tau) nested_mean(1, c(0, 1), c(tau, 1 - tau))</pre>
agmean_index(0.25)(x, w1, w1)
#---- Walsh index ----
# The (arithmetic) Walsh index is the implicit price index when using a
# superlative quadratic mean quantity index of order 1
p1 <- price6[[2]]
p0 <- price6[[1]]
```

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```
q1 <- quantity6[[2]]</pre>
q0 <- quantity6[[1]]</pre>
walsh <- quadratic_mean_index(1)</pre>
sum(p1 * q1) / sum(p0 * q0) / walsh(q1 / q0, p0 * q0, p1 * q1)
sum(p1 * sqrt(q1 * q0)) / sum(p0 * sqrt(q1 * q0))
# Counter to the PPI manual (par. 1.105), it is not a superlative
# quadratic mean price index of order 1
walsh(p1 / p0, p0 * q0, p1 * q1)
# That requires using the average value share as weights
walsh_weights <- sqrt(scale_weights(p0 * q0) * scale_weights(p1 * q1))</pre>
walsh(p1 / p0, walsh_weights, walsh_weights)
#---- Missing values ----
x[1] \leftarrow NA
w1[2] <- NA
fisher_mean(x, w1, w2, na.rm = TRUE)
# Same as using obs 2 and 3 in an arithmetic mean, and obs 3 in a
# harmonic mean
geometric_mean(c(
  arithmetic_mean(x, w1, na.rm = TRUE),
  harmonic_mean(x, w2, na.rm = TRUE)
# Use balanced() to use only obs 3 in both inner means
balanced(fisher_mean)(x, w1, w2, na.rm = TRUE)
```

outliers

Outlier detection for price relatives

### **Description**

Standard cutoff-based methods for detecting outliers with price relatives.

#### Usage

```
quartile_method(x, cu = 2.5, cl = cu, a = 0, type = 7)
```

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```
resistant_fences(x, cu = 2.5, cl = cu, a = 0, type = 7)
robust_z(x, cu = 2.5, cl = cu)
fixed_cutoff(x, cu = 2.5, cl = 1/cu)
tukey_algorithm(x, cu = 2.5, cl = cu, type = 7)
hb_transform(x)
```

### Arguments

X	A strictly positive numeric vector of price relatives. These can be made with, e.g., back_period().
cu, cl	A numeric vector, or something that can be coerced into one, giving the upper and lower cutoffs for each element of x. Recycled to the same length as x.
a	A numeric vector, or something that can be coerced into one, between 0 and 1 giving the scale factor for the median to establish the minimum dispersion between quartiles for each element of x. The default does not set a minimum dispersion. Recycled to the same length as x.
type	See quantile().

#### **Details**

Each of these functions constructs an interval of the form  $[b_l(x) - c_l \times l(x), b_u(x) + c_u \times u(x)]$  and assigns a value in x as TRUE if that value does not belong to the interval, FALSE otherwise. The methods differ in how they construct the values  $b_l(x)$ ,  $b_u(x)$ , l(x), and u(x). Any missing values in x are ignored when calculating the cutoffs, but will return NA.

The fixed cutoff method is the simplest, and just uses the interval  $[c_l, c_u]$ .

The quartile method and Tukey algorithm are described in paragraphs 5.113 to 5.135 of the CPI manual (2020), as well as by Rais (2008) and Hutton (2008). The resistant fences method is an alternative to the quartile method, and is described by Rais (2008) and Hutton (2008). Quantile-based methods often identify price relatives as outliers because the distribution is concentrated around 1; setting a > 0 puts a floor on the minimum dispersion between quantiles as a fraction of the median. See the references for more details.

The robust Z-score is the usual method to identify relatives in the (asymmetric) tails of the distribution, simply replacing the mean with the median, and the standard deviation with the median absolute deviation.

These methods often assume that price relatives are symmetrically distributed (if not Gaussian). As the distribution of price relatives often has a long right tail, the natural logarithm can be used to transform price relative before identifying outliers (sometimes under the assumption that price relatives are distributed log-normal). The Hidiroglou-Berthelot transformation is another approach, described in the CPI manual (par. 5.124). (Sometimes the transformed price relatives are multiplied by  $\max(p_1, p_0)^u$ , for some  $0 \le u \le 1$ , so that products with a larger price get flagged as outliers (par. 5.128).)

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### Value

A logical vector, the same length as x, that is TRUE if the corresponding element of x is identified as an outlier, FALSE otherwise.

### References

Hutton, H. (2008). Dynamic outlier detection in price index surveys. *Proceedings of the Survey Methods Section: Statistical Society of Canada Annual Meeting*.

IMF, ILO, Eurostat, UNECE, OECD, and World Bank. (2020). *Consumer Price Index Manual: Concepts and Methods*. International Monetary Fund.

Rais, S. (2008). Outlier detection for the Consumer Price Index. *Proceedings of the Survey Methods Section: Statistical Society of Canada Annual Meeting.* 

### See Also

grouped() to make each of these functions operate on grouped data.

back\_period()/base\_period() for a simple utility function to turn prices in a table into price relatives.

The HBmethod() function in the **univOutl** package for the Hidiroglou-Berthelot method for identifying outliers.

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price\_data

Sample price/quantity data

# Description

Prices and quantities for six products over five periods.

### **Format**

Each data frame has 6 rows and 5 columns, with each row corresponding to a product and each column corresponding to a time period.

#### Note

Adapted from tables 3.1 and 3.2 in Balk (2008), which were adapted from tables 19.1 and 19.2 in the PPI manual.

#### Source

Balk, B. M. (2008). Price and Quantity Index Numbers. Cambridge University Press.

ILO, IMF, OECD, UNECE, and World Bank. (2004). *Producer Price Index Manual: Theory and Practice*. International Monetary Fund.

```
# Recreate tables 3.4, 3.6, and 3.12 from Balk (2008)
index_formulas <- function(p1, p0, q1, q0) {</pre>
   harmonic_laspeyres = harmonic_index("Laspeyres")(p1, p0, q0),
   geometric_laspeyres = geometric_index("Laspeyres")(p1, p0, q0),
   laspeyres = arithmetic_index("Laspeyres")(p1, p0, q0),
   paasche = harmonic_index("Paasche")(p1, p0, q1),
   geometric_paasche = geometric_index("Paasche")(p1, p0, q1),
   palgrave = arithmetic_index("Palgrave")(p1, p0, q1),
   fisher = fisher_index(p1, p0, q1, q0),
   tornqvist = geometric_index("Tornqvist")(p1, p0, q1, q0),
   marshall_edgeworth = arithmetic_index("MarshallEdgeworth")(p1, p0, q1, q0),
   walsh1 = arithmetic_index("Walsh1")(p1, p0, q1, q0),
   vartia2 = geometric_index("Vartia2")(p1, p0, q1, q0),
   vartia1 = geometric_index("Vartia1")(p1, p0, q1, q0),
    stuvel = stuvel\_index(2, 2)(p1, p0, q1, q0)
round(t(mapply(index_formulas, price6, price6[1], quantity6, quantity6[1])), 4)
```

36 price\_indexes

price\_indexes

Price indexes

### **Description**

Calculate a variety of price indexes using information on prices and quantities at two points in time.

# Usage

```
arithmetic_index(type)
geometric_index(type)
harmonic_index(type)
laspeyres_index(p1, p0, q0, na.rm = FALSE)
paasche_index(p1, p0, q1, na.rm = FALSE)
jevons_index(p1, p0, na.rm = FALSE)
lowe_index(p1, p0, qb, na.rm = FALSE)
young_index(p1, p0, pb, qb, na.rm = FALSE)
fisher_index(p1, p0, q1, q0, na.rm = FALSE)
hlp_index(p1, p0, q1, q0, na.rm = FALSE)
lm_index(elasticity)
cswd_index(p1, p0, na.rm = FALSE)
cswdb_index(p1, p0, q1, q0, na.rm = FALSE)
bw_index(p1, p0, na.rm = FALSE)
stuvel_index(a, b)
arithmetic_agmean_index(elasticity)
geometric_agmean_index(elasticity)
lehr_index(p1, p0, q1, q0, na.rm = FALSE)
```

# **Arguments**

type

The name of the index. See details for the possible types of indexes.

p1	Current-period prices.
p0	Base-period prices.
q0	Base-period quantities.
na.rm	Should missing values be removed? By default missing values for prices or quantities return a missing value.
q1	Current-period quantities.
qb	Period-b quantities for the Lowe/Young index.
pb	Period-b prices for the Lowe/Young index.
elasticity	The elasticity of substitution for the Lloyd-Moulton and AG mean indexes.
a, b	Parameters for the generalized Stuvel index.

## **Details**

The arithmetic\_index(), geometric\_index(), and harmonic\_index() functions return a function to calculate a given type of arithmetic, geometric (logarithmic), and harmonic index. Together, these functions produce functions to calculate the following indexes.

## • Arithmetic indexes

- Carli
- Dutot
- Laspeyres
- Palgrave
- Unnamed index (arithmetic mean of Laspeyres and Palgrave)
- Drobisch (or Sidgwick, arithmetic mean of Laspeyres and Paasche)
- Walsh-I (arithmetic Walsh)
- Marshall-Edgeworth
- Geary-Khamis
- Lowe
- Young
- Hybrid-CSWD
- Geometric indexes
- Jevons
- Geometric Laspeyres (or Jöhr)
- Geometric Paasche
- Geometric Young
- Törnqvist (or Törnqvist-Theil)
- Montgomery-Vartia / Vartia-I
- Sato-Vartia / Vartia-II
- Walsh-II (geometric Walsh)
- Theil

- Rao
- Harmonic indexes
- Coggeshall (equally weighted harmonic index)
- Paasche
- Harmonic Laspeyres
- · Harmonic Young

Along with the lm\_index() function to calculate the Lloyd-Moulton index, these are just convenient wrappers for generalized\_mean() and index\_weights().

The Laspeyres, Paasche, Jevons, Lowe, and Young indexes are among the most common price indexes, and so they get their own functions. The laspeyres\_index(), lowe\_index(), and young\_index() functions correspond to setting the appropriate type in arithmetic\_index(); paasche\_index() and jevons\_index() instead come from the harmonic\_index() and geometric\_index() functions.

In addition to these indexes, there are also functions for calculating a variety of indexes not based on generalized means. The Fisher index is the geometric mean of the arithmetic Laspeyres and Paasche indexes; the Harmonic Laspeyres Paasche (or Harmonic Paasche Laspeyres) index is the harmonic analog of the Fisher index (8054 on Fisher's list). The Carruthers-Sellwood-Ward-Dalen and Carruthers-Sellwood-Ward-Dalen-Balk indexes are sample analogs of the Fisher index; the Balk-Walsh index is the sample analog of the Walsh index. The AG mean index is the arithmetic or geometric mean of the geometric and arithmetic Laspeyres indexes, weighted by the elasticity of substitution. The stuvel\_index() function returns a function to calculate a Stuvel index of the given parameters. The Lehr index is an alternative to the Geary-Khamis index, and is the implicit price index for Fisher's index 4153.

#### Value

arithmetic\_index(), geometric\_index(), harmonic\_index(), and stuvel\_index() each return a function to compute the relevant price indexes; lm\_index(), arithmetic\_agmean\_index(), and geometric\_agmean\_index() each return a function to calculate the relevant index for a given elasticity of substitution. The others return a numeric value giving the change in price between the base period and current period.

## Note

There are different ways to deal with missing values in a price index, and care should be taken when relying on these functions to remove missing values. Setting na.rm = TRUE removes price relatives with missing information, either because of a missing price or a missing weight, while using all available non-missing information to make the weights.

Certain properties of an index-number formula may not work as expected when removing missing values if there is ambiguity about how to remove missing values from the weights (as in, e.g., a Törnqvist or Sato-Vartia index). The balanced() operator may be helpful, as it balances the removal of missing values across prices and quantities prior to making the weights.

#### References

Balk, B. M. (2008). Price and Quantity Index Numbers. Cambridge University Press.

Fisher, I. (1922). The Making of Index Numbers. Houghton Mifflin Company.

IMF, ILO, Eurostat, UNECE, OECD, and World Bank. (2020). *Consumer Price Index Manual: Concepts and Methods*. International Monetary Fund.

von der Lippe, P. (2007). *Index Theory and Price Statistics*. Peter Lang.

von der Lippe, P. (2015). Generalized Statistical Means and New Price Index Formulas, Notes on some unexplored index formulas, their interpretations and generalizations. Munich Personal RePEc Archive paper no. 64952.

Selvanathan, E. A. and Rao, D. S. P. (1994). Index Numbers: A Stochastic Approach. MacMillan.

#### See Also

```
generalized_mean() for the generalized mean that powers most of these functions.
contributions() for calculating percent-change contributions.
quantity_index() to remap the arguments in these functions for a quantity index.
```

price6() for an example of how to use these functions with more than two time periods.

The **piar** package has more functionality working with price indexes for multiple groups of products over many time periods.

Other price index functions: geks(), index\_weights(), splice\_index()

```
p0 <- price6[[2]]</pre>
p1 <- price6[[3]]
q0 <- quantity6[[2]]</pre>
q1 <- quantity6[[3]]</pre>
pb <- price6[[1]]</pre>
qb <- quantity6[[1]]
#---- Calculating price indexes ----
# Most indexes can be calculated by combining the appropriate weights
# with the correct type of mean
geometric_index("Laspeyres")(p1, p0, q0)
geometric_mean(p1 / p0, index_weights("Laspeyres")(p0, q0))
# Arithmetic Laspeyres index
laspeyres_index(p1, p0, q0)
arithmetic_mean(p1 / p0, index_weights("Laspeyres")(p0, q0))
# Harmonic calculation for the arithmetic Laspeyres
harmonic_mean(p1 / p0, index_weights("HybridLaspeyres")(p1, q0))
```

```
# Same as transmuting the weights
all.equal(
  scale_weights(index_weights("HybridLaspeyres")(p1, q0)),
  transmute_weights(1, -1)(p1 / p0, index_weights("Laspeyres")(p0, q0))
)
# This strategy can be used to make more exotic indexes, like the
# quadratic-mean index (von der Lippe, 2007, p. 61)
generalized_mean(2)(p1 / p0, index_weights("Laspeyres")(p0, q0))
# Or the exponential mean index (p. 62)
log(arithmetic_mean(exp(p1 / p0), index_weights("Laspeyres")(p0, q0)))
# Or the arithmetic hybrid index (von der Lippe, 2015, p. 5)
arithmetic_mean(p1 / p0, index_weights("HybridLaspeyres")(p1, q0))
contraharmonic_mean(p1 / p0, index_weights("Laspeyres")(p0, q0))
# Unlike its arithmetic counterpart, the geometric Laspeyres can
# increase when base-period prices increase if some of these prices
# are small
gl <- geometric_index("Laspeyres")</pre>
p0_small <- replace(p0, 1, p0[1] / 5)</pre>
p0_dx \leftarrow replace(p0_small, 1, p0_small[1] + 0.01)
gl(p1, p0\_small, q0) < gl(p1, p0\_dx, q0)
#---- Price updating the weights in a price index ----
# Chain an index by price updating the weights
p2 <- price6[[4]]</pre>
laspeyres_index(p2, p0, q0)
I1 <- laspeyres_index(p1, p0, q0)</pre>
w_pu <- update_weights(p1 / p0, index_weights("Laspeyres")(p0, q0))</pre>
I2 <- arithmetic_mean(p2 / p1, w_pu)</pre>
I1 * I2
# Works for other types of indexes, too
harmonic_index("Laspeyres")(p2, p0, q0)
I1 <- harmonic_index("Laspeyres")(p1, p0, q0)</pre>
w_pu <- factor_weights(-1)(p1 / p0, index_weights("Laspeyres")(p0, q0))</pre>
I2 <- harmonic_mean(p2 / p1, w_pu)</pre>
I1 * I2
#---- Percent-change contributions ----
```

```
# Percent-change contributions for the Tornqvist index
w <- index_weights("Tornqvist")(p1, p0, q1, q0)</pre>
(con <- geometric_contributions(p1 / p0, w))</pre>
all.equal(sum(con), geometric_index("Tornqvist")(p1, p0, q1, q0) - 1)
#---- Missing values ----
# NAs get special treatment
p_na <- replace(p0, 6, NA)</pre>
# Drops the last price relative
laspeyres_index(p1, p_na, q0, na.rm = TRUE)
# Only drops the last period-0 price
sum(p1 * q0, na.rm = TRUE) / sum(p_na * q0, na.rm = TRUE)
#---- von Bortkiewicz decomposition ----
paasche_index(p1, p0, q1) / laspeyres_index(p1, p0, q0) - 1
wl <- scale_weights(index_weights("Laspeyres")(p0, q0))</pre>
pl <- laspeyres_index(p1, p0, q0)</pre>
ql <- quantity_index(laspeyres_index)(q1, q0, p0)</pre>
sum(wl * (p1 / p0 / pl - 1) * (q1 / q0 / ql - 1))
# Similar decomposition for geometric Laspeyres/Paasche
wp <- scale_weights(index_weights("Paasche")(p1, q1))</pre>
gl <- geometric_index("Laspeyres")(p1, p0, q0)</pre>
gp <- geometric_index("Paasche")(p1, p0, q1)</pre>
log(gp / gl)
sum(scale\_weights(wl) * (wp / wl - 1) * log(p1 / p0 / gl))
#---- Consistency in aggregation ----
p0a <- p0[1:3]
p0b <- p0[4:6]
p1a <- p1[1:3]
p1b \leftarrow p1[4:6]
q0a <- q0[1:3]
q0b <- q0[4:6]
q1a <- q1[1:3]
q1b \leftarrow q1[4:6]
# Indexes based on the generalized mean with value share weights are
```

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```
# consistent in aggregation
lm_index(0.75)(p1, p0, q0)
w <- index_weights("LloydMoulton")(p0, q0)</pre>
Ia <- generalized_mean(0.25)(p1a / p0a, w[1:3])
Ib <- generalized_mean(0.25)(p1b / p0b, w[4:6])
generalized_mean(0.25)(c(Ia, Ib), c(sum(w[1:3]), sum(w[4:6])))
# Agrees with group-wise indexes
all.equal(lm_index(0.75)(p1a, p0a, q0a), Ia)
all.equal(lm_index(0.75)(p1b, p0b, q0b), Ib)
# Care is needed with more complex weights, e.g., Drobisch, as this
# doesn't fit Balk's (2008) definition (p. 113) of a generalized-mean
# index (it's the arithmetic mean of a Laspeyres and Paasche index)
arithmetic_index("Drobisch")(p1, p0, q1, q0)
w <- index_weights("Drobisch")(p1, p0, q1, q0)</pre>
Ia <- arithmetic_mean(p1a / p0a, w[1:3])</pre>
Ib <- arithmetic_mean(p1b / p0b, w[4:6])</pre>
arithmetic_mean(c(Ia, Ib), c(sum(w[1:3]), sum(w[4:6])))
# Does not agree with group-wise indexes
all.equal(arithmetic_index("Drobisch")(p1a, p0a, q1a, q0a), Ia)
all.equal(arithmetic_index("Drobisch")(p1b, p0b, q1b, q0b), Ib)
```

quantity\_index

Quantity index operator

## Description

Remaps price arguments into quantity argument (and vice versa) to turn a price index into a quantity index.

#### Usage

```
quantity_index(f)
```

## **Arguments** f

A price-index function.

## Value

A function like f, except that the role of prices/quantities is reversed.

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## See Also

Other operators: balanced(), grouped()

## **Examples**

```
p1 <- price6[[3]]
p0 <- price6[[2]]
q1 <- quantity6[[3]]
q0 <- quantity6[[2]]

# Remap argument names to be quantities rather than prices
quantity_index(laspeyres_index)(q1 = q1, q0 = q0, p0 = p0)
laspeyres_index(p1 = q1, p0 = q0, q0 = p0)

# Works with the index_weights() functions, too
quantity_index(index_weights("Laspeyres"))(q0 = q0, p0 = p0)</pre>
```

scale\_weights

Scale weights

## **Description**

Scale a vector of weights so that they sum to 1.

## Usage

```
scale_weights(x)
```

#### **Arguments**

Χ

A strictly positive numeric vector.

## Value

A numeric vector that sums to 1. If there are NAs in x then the result sums 1 to if these values are removed.

## See Also

```
grouped() to make this function applicable to grouped data.
Other weights functions: factor_weights(), transmute_weights()
```

```
scale_weights(1:5)
```

splice\_index

splice_index	Splice an index series	
--------------	------------------------	--

## **Description**

Splice a collection of index series computed over a rolling window into one index series. Splicing on multiple points combines the results with a geometric mean.

## Usage

```
splice_index(x, periods = NULL, initial = NULL, published = FALSE)
```

## Arguments

x	A list of equal-length numeric vectors giving the period-over-period indexes for each window.
periods	An integer vector giving the splice points for each window. The default splices on each point in the window.
initial	A numeric vector giving an initial period-over-period index series onto which the elements of x are spliced. The default uses the first element of x.
published	Should the splice be done against the published series? The default splices using the recalculated index series.

## Value

A numeric vector giving the spliced (fixed-base) index series.

## References

Chessa, A. G. (2019). A Comparison of Index Extension Methods for Multilateral Methods. Paper presented at the 16th Meeting of the Ottawa Group on Price Indices, 8-10 May 2019, Rio de Janeiro, Brazil.

Krsinich, F. (2016). The FEWS index: Fixed effects with a window splice. *Journal of Official Statistics*, 32(2), 375-404.

## See Also

Other price index functions: geks(), index\_weights(), price\_indexes

```
# Make an index series over a rolling window
x <- list(c(1.1, 0.9, 1.2), c(0.8, 1.3, 1.4), c(1.3, 1.3, 0.8))
# Mean splice
splice_index(x)</pre>
```

```
# Movement splice
splice_index(x, 3)
# Window splice
splice_index(x, 1)
# Splicing on the published series preserves the within-window
# movement of the index series
splice_index(x, 1, published = TRUE)
```

transmute\_weights

Transmute weights

## **Description**

Transmute weights to turn a generalized mean of order r into a generalized mean of order s. Useful for calculating additive and multiplicative decompositions for a generalized-mean index, and those made of nested generalized means (e.g., Fisher index).

## Usage

```
transmute_weights(r, s)
nested_transmute(r1, r2, s, t = c(1, 1))
nested_transmute2(r1, r2, s, t = c(1, 1))
```

## **Arguments**

r, s A finite number giving the order of the generalized mean. See details.

r1 A finite number giving the order of the outer generalized mean.

r2 A pair of finite numbers giving the order of the inner generalized means.

t A pair of strictly positive weights for the inner generalized means. The default is equal weights.

## Details

The function transmute\_weights(r, s) returns a function to compute a vector of weights v(x, w) such that

```
generalized_mean(r)(x, w) == generalized_mean(s)(x, v(x, w))
```

nested\_transmute(r1, r2, t, s) and nested\_transmute2(r1, r2, t, s) do the same for nested generalized means, so that

```
nested_mean(r1, r2, t)(x, w1, w2) == generalized_mean(s)(x, v(x, w1, w2))
```

This generalizes the result for turning a geometric mean into an arithmetic mean (and vice versa) in section 4.2 of Balk (2008), and a Fisher mean into an arithmetic mean in section 6 of Reinsdorf et al. (2002), although these are usually the most important cases. See Martin (2021) for details. nested\_transmute2() takes a slightly different approach than nested\_transmute(), generalizing the van IJzeren arithmetic decomposition for the Fisher index (Balk, 2008, section 4.2.2) using the approach by Martin (2021), although in most cases the results are broadly similar.

Transmuting weights returns a value that is the same length as x, so any missing values in x or the weights will return NA. Unless all values are NA, however, the result for will still satisfy the above identities when na.rm = TRUE.

#### Value

```
transmute_weights() returns a function:
function(x, w = NULL){...}

nested_transmute() and nested_transmute2() similarly return a function:
function(x, w1 = NULL, w2 = NULL){...}
```

## References

Balk, B. M. (2008). Price and Quantity Index Numbers. Cambridge University Press.

Martin, S. (2021). A note on general decompositions for price indexes. *Prices Analytical Series*, Statistics Canada catalogue no. 62F0014M. Statistics Canada, Ottawa.

Reinsdorf, M. B., Diewert, W. E., and Ehemann, C. (2002). Additive decompositions for Fisher, Törnqvist and geometric mean indexes. *Journal of Economic and Social Measurement*, 28(1-2):51–61.

Sydsaeter, K., Strom, A., and Berck, P. (2005). *Economists' Mathematical Manual* (4th edition). Springer.

## See Also

```
generalized_mean() for the generalized mean and nested_mean() for the nested mean.
extended_mean() for the extended mean that underlies transmute_weights().
contributions() for calculating additive percent-change contributions.
grouped() to make these functions operate on grouped data.
Other weights functions: factor_weights(), scale_weights()
```

```
x < -1:3
v <- 4:6
w <- 3:1
#---- Transforming generalized means ----
# Calculate the geometric mean as an arithmetic mean and
# harmonic mean by transmuting the weights
geometric_mean(x)
arithmetic_mean(x, transmute_weights(0, 1)(x))
harmonic_mean(x, transmute_weights(0, -1)(x))
# Transmuting the weights for a harmonic mean into those
\# for an arithmetic mean is the same as using weights w / x
all.equal(transmute_weights(-1, 1)(x, w), scale_weights(w / x))
# Transmuting the weights for an arithmetic mean into those
\# for a harmonic mean is the same as using weights w * x
all.equal(transmute_weights(1, -1)(x, w), scale_weights(w * x))
# Works for nested means, too
w1 <- 3:1
w2 <- 1:3
fisher_mean(x, w1, w2)
arithmetic_mean(x, nested_transmute(0, c(1, -1), 1)(x, w1, w2))
arithmetic_mean(x, nested_transmute2(0, c(1, -1), 1)(x, w1, w2))
# Note that nested_transmute() has an invariance property
# not shared by nested_transmute2()
all.equal(
  nested_transmute(0, c(1, -1), 1)(x, w1, w2),
  transmute_weights(2, 1)(
    x, nested_transmute(0, c(1, -1), 2)(x, w1, w2)
  )
)
all.equal(
  nested_transmute2(0, c(1, -1), 1)(x, w1, w2),
  transmute_weights(2, 1)(
    x, nested_transmute2(0, c(1, -1), 2)(x, w1, w2)
  )
)
#---- Monotonicity ----
```

```
\# Transmuted weights increase when x is small and decrease
# when x is large if r < s
transmute_weights(0, 1)(x, w) > scale_weights(w)
# The opposite happens when r > s
transmute_weights(1, \theta)(x, w) > scale_weights(w)
#---- Percent-change contributions ----
# Transmuted weights can be used to calculate percent-change
# contributions for, e.g., a geometric price index
transmute_weights(0, 1)(x) * (x - 1)
geometric_contributions(x) # the more convenient way
#---- Basket representation of a price index ----
# Any generalized-mean index can be represented as a basket-style
# index by transmuting the weights, which is how some authors
# define a price index (e.g., Sydsaeter et al., 2005, p. 174)
p1 <- 2:6
p0 <- 1:5
qs <- transmute_weights(-1, 1)(p1 / p0) / p0
all.equal(harmonic_mean(p1 / p0), sum(p1 * qs) / sum(p0 * qs))
```

# **Index**

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